



SYNCHROTRON RADIATION AND LIGHT SOURCES

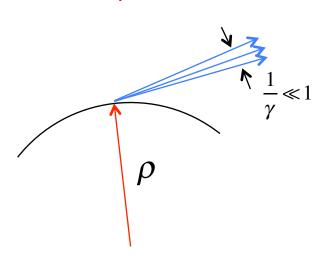
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Synchrotron Radiation

For a relativistic particle, the total radiated power (S&E 8.1) is



$$a = \operatorname{acceleration} = \frac{v^{2}}{\rho} \approx \frac{c^{2}}{\rho}$$

$$P = \frac{1}{6\pi\epsilon_{0}} \frac{e^{2}a^{2}}{c^{3}} \gamma^{4}$$

$$\approx \frac{1}{6\pi\epsilon_{0}} \frac{e^{2}c}{\rho^{2}} \gamma^{4} = \frac{1}{6\pi\epsilon_{0}} \frac{e^{2}c}{\rho^{2}} \left(\frac{E}{m_{0}c^{2}}\right)^{4}$$

In a magnetic field

$$\rho = \frac{m\gamma c}{eB} \longrightarrow P = \frac{e^4}{6\pi\epsilon_0} \frac{B^2}{m_0^2 c} \gamma^2$$
$$= \frac{e^4}{6\pi\epsilon_0 m^4 c^5} B^2 E^2$$

Electron radiates 10¹³ times more than a proton of the same energy!





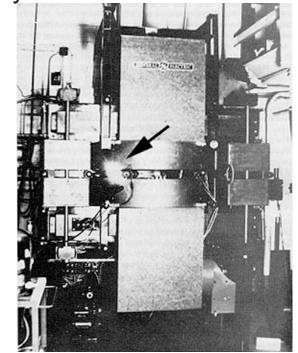
First Observation of Synchrotron Radiation

 The first attempt to observe synchrotron radiation was in 1944 at the 100 MeV GE betatron

 Because of a miscalculation, they were looking in the microwave region rather than the visible (in fact the walls were opaque), so although the say an energy decay, they did not observe the

radiation.

 Synchrotron radiation was first successfully observed in 1947 by Elder, Gurewitsch, and Langmuir at the GE 70 MeV electron synchrotron.

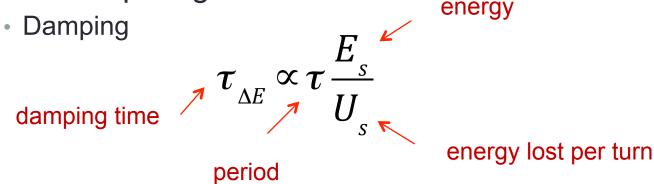






Effects of Synchrotron Radiation

Two competing effects



Quantum "heating" effects related to the statistics of the photons

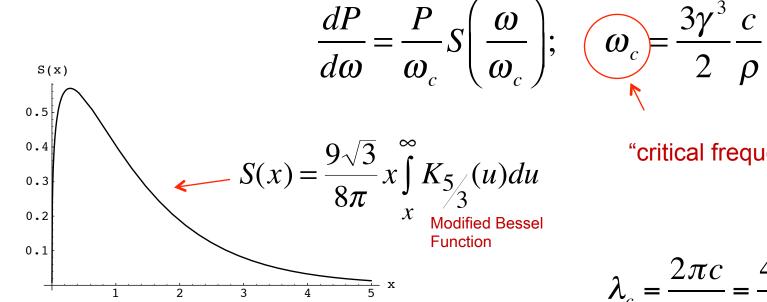
$$N_p = \dot{N}\tau \quad \to \quad \sigma_{\Delta E} = \sqrt{\dot{N}\tau_{\Delta E}\left\langle u^2\right\rangle}$$
 Number of photons per period Rate of photon emission Average photon energy





Power Spectrum of Synchrotron Radiation

The power spectrum of radiation is given by



"critical frequency"

Differential photon rate

$$\dot{n} = \frac{d\dot{N}}{du}$$

"critical wavelength"

"critical energy"





Some Handy Numbers (don't bother to memorize)

The total rate is:

USPAS Fundamentals, June 4-15, 2018

$$\dot{N} = \int_0^\infty \dot{n}(u)du = \frac{15\sqrt{3}}{8} \frac{P}{u_c}$$

The mean photon energy is then

$$\langle u \rangle = \frac{P}{\dot{N}} = \frac{8}{15\sqrt{3}} u_c$$

The mean square of the photon energy is

$$\langle u^2 \rangle = \frac{1}{\dot{N}} \int_0^\infty u^2 \dot{n}(u) du = \frac{P}{\dot{N}} \int_0^\infty \frac{u}{u_c} S\left(\frac{u}{u_c}\right) du$$
$$= \frac{11}{27} u_c^2$$

The energy lost per turn is

$$U_{s} = \oint P dt = \frac{e^{2} c \gamma^{4}}{6\pi \epsilon_{0}} \oint \frac{1}{\rho^{2}} \left(\frac{dt}{ds}\right) ds$$
$$= \frac{e^{2} \gamma^{4}}{6\pi \epsilon_{0}} \oint \frac{1}{\rho^{2}} ds$$





Example: The Failed Experiment

- In 1944 GE looked for synchrotron radiation in a 100 MeV electron beam.
 - Assume B=1T
- We have
 - E≈pc=100 MeV
 - mc²=.511 MeV
 - $\gamma = E/(mc^2) = 196$
 - $(B\rho)=100/300=.333 \text{ T-m}$
 - $\rho = (B\rho)/B = .333 \text{ m}$

eV-m
$$u_{c} = \frac{3\gamma^{3}}{2} \frac{(\hbar c)}{\rho} = \frac{3(196)^{3}(1.97 \times 10^{-7})}{2(.333)} = 6.6 \text{ eV}$$

$$\langle u \rangle = \frac{8}{15\sqrt{3}} u_{c} = 2.05 \text{ eV}$$

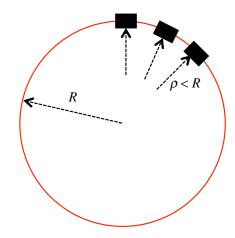
$$eV-\mu m$$

$$\lambda_{\langle u \rangle} = \frac{(hc)}{\langle u \rangle} = \frac{1.2}{2.05} = .587 \mu m$$
Visible yellow light, NOT microwaves





It's important to remember that ρ is *not* the curvature of the accelerator as a whole, but rather the curvature of individual magnets.



$\Delta\theta = \frac{\Delta s}{\rho} \to \oint \frac{ds}{\rho} = 2\pi$

So if an accelerator is built using magnets of a fixed radius ρ_0 , then the energy lost per turn is

$$U_{s} = \frac{e^{2}\gamma^{4}}{6\pi\epsilon_{0}} \oint \frac{1}{\rho^{2}} ds = \frac{e^{2}\gamma^{4}}{6\pi\epsilon_{0}\rho_{0}} \oint \frac{1}{\rho} ds = \frac{e^{2}\gamma^{4}}{3\epsilon_{0}\rho_{0}}$$
"isomagnetic"

For electrons

$$U_{s}[\text{MeV}] = .0885 \frac{E^{4}[\text{GeV}]}{\rho_{0}[\text{m}]}$$

$$u_{c} = \hbar \omega_{c} = \frac{3\gamma^{3}\hbar}{2} \frac{c}{\rho_{0}}$$

$$u_{c}[\text{keV}] = 2.218 \frac{E^{3}[\text{GeV}]}{\rho_{0}[\text{m}]}$$

$$N_{s} = \dot{N}\tau = \frac{15\sqrt{3}}{8} \frac{P}{u_{c}}\tau = \frac{15\sqrt{3}}{8} \frac{U_{s}}{u_{c}}$$
photons/turn
$$= .1296 E[\text{GeV}]$$

Example: CESR

$$E = 5.29 \text{ GeV}$$

$$\rho_0 = 98 \text{ m}$$

$$U_s = .71 \text{ MeV}$$

$$\langle u \rangle = \frac{8}{15\sqrt{3}} u_c = .98 \text{ keV}$$

$$\sqrt{\langle u^2 \rangle} = \sqrt{\frac{11}{27}} u_c = 2.0 \text{ keV}$$

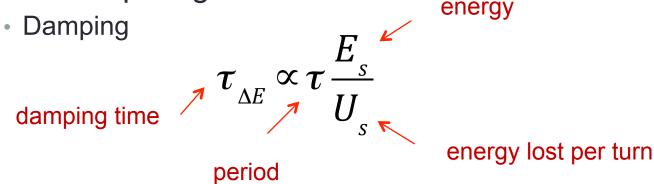
$$N_s = 721$$





Effects of Synchrotron Radiation

Two competing effects



Quantum "heating" effects related to the statistics of the photons

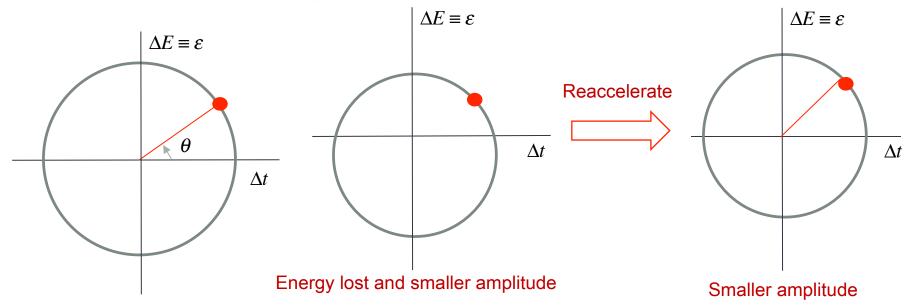
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 Number of photons per period Rate of photon emission Average photon energy





Small Amplitude Longitudinal Motion

 $P \propto E^2$ \rightarrow Particles lose more energy at the top of this cycle than the bottom



$$\left\langle \frac{d\varepsilon_{0}^{2}}{dt} \right\rangle = \frac{1}{\tau_{s}} \oint \frac{d\varepsilon_{0}^{2}}{dt} dt$$

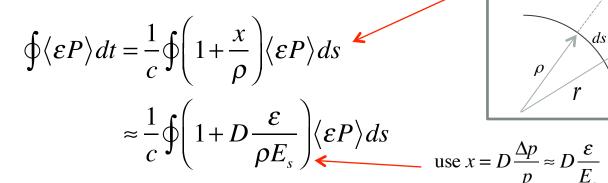
$$= -\frac{2}{\tau_{s}} \oint \left\langle \varepsilon P \right\rangle dt + \frac{1}{\tau_{s}} \oint \dot{N} \left\langle u^{2} \right\rangle dt$$

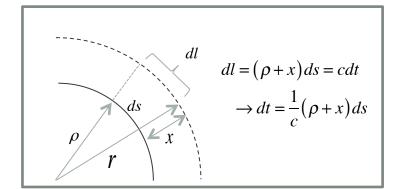
$$= \text{damping term}$$
Heating term due to statistical fluctuations





Evaluate integral in damping term





Recall

$$P = \frac{e^4}{6\pi\epsilon_0 m^4 c^5} B^2 E^2 \rightarrow \frac{dP}{dE} = 2P \left(\frac{1}{B_0} \frac{dB}{dE} + \frac{1}{E} \right)$$

$$P(\varepsilon) = P_s + \frac{dP}{dE} \varepsilon = P_s \left(1 + 2 \left(\frac{1}{B_0} \frac{dB}{dE} + \frac{1}{E_s} \right) \varepsilon \right)$$

Can't ignore anything!!

Dependence of field

$$P = \frac{e^4}{6\pi\epsilon_0 m^4 c^5} B^2 E^2 \to \frac{dP}{dE} = 2P \left(\frac{1}{B_0} \frac{dB}{dE} + \frac{1}{E} \right) \qquad \frac{dB}{dx} = B' \qquad \frac{dB}{dE} = \frac{dB}{dx} \frac{dx}{dE}$$

$$= \kappa \left(B\rho \right) \qquad = \frac{\kappa \left(B\rho \right) D}{E_s}$$

$$\rightarrow P(\varepsilon) = P_s \left(1 + \frac{2\varepsilon}{E_s} (\kappa \rho D + 1) \right)$$





Putting it all together...

$$\oint \langle \varepsilon P \rangle dt = \frac{1}{c} \oint \left\langle \varepsilon P_s \left(1 + \frac{\varepsilon}{E_s} \frac{D}{\rho} \right) \left(1 + \frac{2\varepsilon}{E_s} (\kappa \rho D + 1) \right) \right\rangle ds$$

$$= \frac{1}{c} \oint \left\langle P_s \left(\varepsilon + \frac{\varepsilon^2}{E_s} \left(2 + 2\kappa \rho D + \frac{D}{\rho} \right) + \varepsilon^2 \frac{2D(\kappa \rho D + 1)}{E_s \rho} \right) \right\rangle ds$$

$$= \frac{1}{c} \frac{\varepsilon_0^2}{2E_s} \oint P_s \left(2 + 2\kappa \rho D + \frac{D}{\rho} \right) ds$$

$$= \frac{\varepsilon_0^2 U_s}{E_s} + \frac{\varepsilon_0^2}{2E_s} \frac{1}{c} \oint P_s \left(2\kappa \rho D + \frac{D}{\rho} \right) ds$$

$$= \frac{\varepsilon_0^2 U_s}{E_s} + \frac{\varepsilon_0^2 U_s}{2E_s} D$$

$$= \frac{\varepsilon_0^2 U_s}{2E_s} (2 + D)$$

$$= \frac{\varepsilon_0^2 U_s}{2E_s} (2 + D)$$

use

$$\varepsilon = \varepsilon_0 \sin(2\pi v_s n + \delta)$$

$$\longrightarrow \langle \varepsilon \rangle = \langle \varepsilon^3 \rangle = 0$$

$$\langle \varepsilon^2 \rangle = \frac{\varepsilon_0^2}{2}$$

note
$$\frac{1}{c} \oint P_s ds = \frac{1}{c} (\text{const}) \oint \frac{1}{\rho^2} ds$$

$$= U_s$$

$$\frac{1}{c} \oint P_s \left(2\kappa \rho D + \frac{D}{\rho} \right) ds = \frac{1}{c} (\text{const}) \oint \frac{1}{\rho^2} \left(2\kappa \rho D + \frac{D}{\rho} \right) ds$$

$$= U_s \mathcal{D}$$
where $\mathcal{D} \equiv \frac{\oint \frac{1}{\rho^2} \left(2\kappa \rho D + \frac{D}{\rho} \right) ds}{\oint \frac{1}{\rho^2} ds}$





Reminder: Damping + Heating

In general, if I have a simple damping force of the form

$$\frac{dA}{dt} = -\lambda A$$

the solution is

$$A(t) = A_0 e^{-\lambda t} = A_0 e^{-t/\tau}$$
; where $\tau = 1/\lambda$

If I add a constant heating term

$$\frac{dA}{dt} = -\lambda A + h$$

$$\int \frac{dA}{A - h/\lambda} = \int -\lambda \, dt$$

$$\Rightarrow \ln(A - h/\lambda) = -\lambda t + K$$

$$\Rightarrow A = Ce^{-\lambda t} + h/\lambda$$

$$A(0) = A_0 \rightarrow C = 1 - h / \lambda$$

$$\rightarrow A(t) = A_0 e^{-\lambda t} + \frac{h}{\lambda} (1 - e^{-\lambda t})$$

$$\rightarrow A(\infty) = \frac{h}{\lambda} = h\tau$$





Result

$$\left\langle \frac{d\varepsilon_0^2}{dt} \right\rangle = -\frac{2}{\tau_s} \oint \left\langle \varepsilon P \right\rangle dt + \frac{1}{\tau_s} \oint \dot{N} \left\langle u^2 \right\rangle dt$$

$$= -\frac{\varepsilon_0^2 U_s}{\tau_s E_s} (2 + \mathcal{D}) + \frac{1}{\tau_s} \oint \dot{N} \left\langle u^2 \right\rangle dt$$
damping heating

where
$$\mathcal{D} = \frac{\oint \frac{1}{\rho^2} \left(2\kappa \rho D + \frac{D}{\rho} \right) ds}{\oint \frac{1}{\rho^2} ds}$$

$$\varepsilon_0^2(t) = \varepsilon_0^2(0)e^{-t/\tau_{\varepsilon^2}} + \varepsilon_0^2(\infty)\left(1 - e^{-t/\tau_{\varepsilon^2}}\right)$$

where $\frac{1}{\tau_{s^2}} = \frac{U_s}{\tau_s E_s} (2 + \mathcal{D})$ The energy then decays in a time

$$\varepsilon_0^2(\infty) = \frac{\tau_{\varepsilon^2}}{\tau_s} \oint \dot{N} \langle u^2 \rangle dt$$

$$\tau_{\varepsilon} = 2\tau_{\varepsilon^{2}}$$

$$\frac{1}{\tau_{\varepsilon}} = \frac{U_{s}}{2\tau_{s}E_{s}}(2+\mathcal{D})$$





Longitudinal Damping in a "Normal" Synchrotron

- So far we have talked about "separated function", "isomagnetic" lattices, which has
 - A single type of dipole: $\kappa = 0; \rho = \rho_0$
 - Quadrupoles: $\kappa \neq 0; \rho = \infty$
- In this case

$$\mathcal{D} = \frac{\oint \frac{1}{\rho^2} \left(2\kappa \rho D + \frac{D}{\rho} \right) ds}{\oint \frac{1}{\rho^2} ds} = \frac{\frac{1}{\rho_0^2} \oint \frac{D}{\rho_0} ds}{\frac{1}{\rho_0} \oint \frac{1}{\rho_0} ds} = \frac{\frac{1}{\rho_0^2} (C\alpha_C)}{\frac{1}{\rho_0} (2\pi)}$$
$$= \frac{C\alpha_C}{2\pi\rho_0} \approx \alpha_C \ll 1$$

$$\frac{1}{\tau_{\varepsilon}} \approx \frac{U_{s}}{\tau_{s} E_{s}}$$

 $\frac{1}{\tau_{\varepsilon}} \approx \frac{U_s}{\tau_s E_s}$ probably the answer you would have guessed without doing any calculations. probably the answer you would





Equilibrium Energy Spread

 We can relate the spread in energy to the peak of the square with

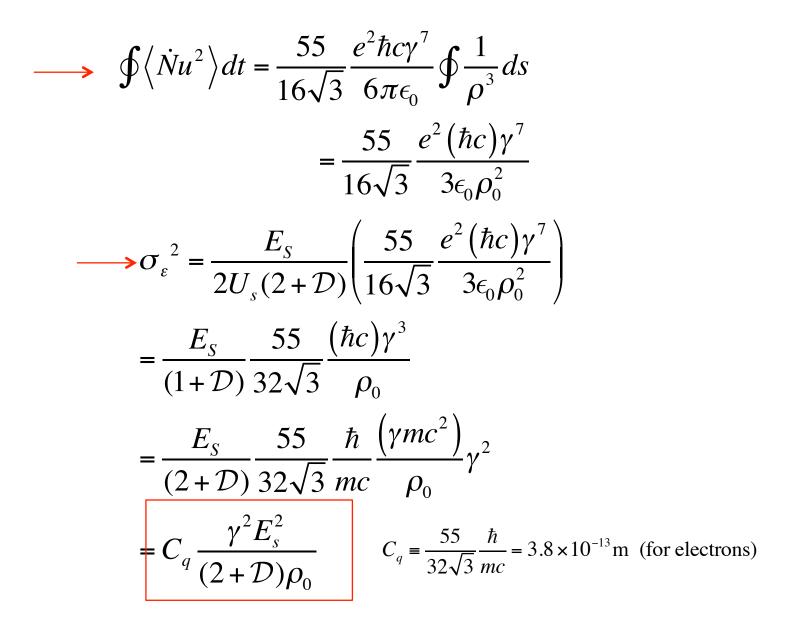
$$\begin{aligned} \sigma_{\varepsilon}^{2} &= \left\langle \varepsilon_{0}^{2}(\infty) \right\rangle = \frac{1}{2} \varepsilon_{0}^{2}(\infty) \\ &= \frac{1}{2} \frac{\tau_{\varepsilon^{2}}}{\tau_{\varepsilon}} \oint \left\langle \dot{N}u^{2} \right\rangle dt = \frac{\tau_{\varepsilon}}{4\tau_{\varepsilon}} \oint \left\langle \dot{N}u^{2} \right\rangle dt = \frac{E_{S}}{2U_{\varepsilon}(2+\mathcal{D})} \oint \left\langle \dot{N}u^{2} \right\rangle dt \end{aligned}$$

Use
$$P = \frac{1}{6\pi\epsilon_0} \frac{e^2 c}{\rho^2} \gamma^4, \dot{N} = \frac{15\sqrt{3}}{8} \frac{P}{u_c}, \quad \langle u^2 \rangle = \frac{11}{27} u_c^2, \quad u_c = \frac{3}{2} \frac{\hbar \gamma^3}{\rho} c$$

$$\tau_{\varepsilon} = \tau_s \frac{2E_s}{U_s(2+\mathcal{D})}, U_s = \frac{e^2 \gamma^4}{3\epsilon_0 \rho_0}$$



This leads to

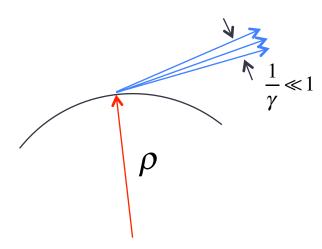






Damping in the Vertical Plane

Synchrotron radiation

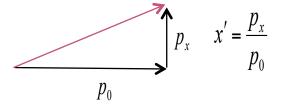


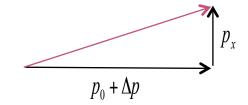
Energy lost along trajectory, so radiated power will reduce momentum along flight path

$$\frac{d\vec{p}}{dt} \approx -\frac{P}{c}\hat{\theta}$$

If we assume that the RF system restores the energy lost each turn, then

Energy lost along the path $\rightarrow \Delta y = \Delta y' = 0$ Energy restored along nominal path \hat{s} \rightarrow "adiabatic damping"









Damping in the Vertical Plan (cont'd)

 The math follows much like the case of adiabatic damping, and we find that

$$\frac{1}{\tau_y} = \frac{1}{2\tau_s} \frac{U_S}{E_S} = \frac{1}{2\tau_\varepsilon}$$

- Unlike the longitudinal plane, there is no heating term, so in the absence of coupling, the emittance would damp to zero in the vertical plane.
 - This turns out to a problem for stability





Horizontal Plane

The horizontal plane has the same damping term as the vertical plane, but it has more contributions because the position depends on energy

betatron motion
$$x = x_{\beta} + D \frac{\epsilon}{E_{s}}$$

$$x_{\beta} = a\sqrt{\beta} \cos(\psi(s) + \delta) \equiv a\sqrt{b}C$$

$$x_{\beta} = a\sqrt{\beta} \cos(\psi(s) + \delta) = a\sqrt{b}C$$

$$x'_{\beta} = -\frac{a}{\sqrt{\beta}} (\alpha \cos(\psi(s) + \delta) + \sin(\psi(s) + \delta)) \equiv -\frac{a}{\sqrt{\beta}} (\alpha C + S)$$

If we radiate a photon of energy u, it will change the energy, but not the position or the angle. $(\varepsilon - u)$ Γ

$$\Delta x = \left[\left(x_{\beta} + \Delta x_{\beta} \right) + D \frac{(\varepsilon - u)}{E_{s}} \right] - \left[x_{\beta} + D \frac{\varepsilon}{E_{s}} \right]$$

$$= \Delta x_{\beta} - D \frac{u}{E_{s}} = 0$$

$$\Delta x_{\beta} = D \frac{u}{E_{s}}$$

$$\Delta x' = \Delta x'_{\beta} - D' \frac{u}{E_{s}} = 0$$

$$\Delta x'_{\beta} = D' \frac{u}{E_{s}}$$





Result in Horizontal Plane

Skipping a lot of math, we get

$$\frac{1}{\tau_{x}} = \frac{U_{s}}{2\tau_{s}E_{s}} (1 - \mathcal{D})$$

$$\approx \frac{U_{s}}{2\tau_{s}E_{s}}$$

where
$$\mathcal{D} = \frac{\oint \frac{1}{\rho^2} \left(2\kappa \rho D + \frac{D}{\rho} \right) ds}{\oint \frac{1}{\rho^2} ds}$$

Same as longitudinal plane

Separated function isomagnetic synchrotrons





Equilibrium Emittance in X

The equilibrium emittance is given by

$$\epsilon_{x}(\infty) = C_{q} \frac{\gamma^{2}}{(1-\mathcal{D})} \frac{\oint \frac{\mathcal{H}}{\rho^{3}} ds}{\oint \frac{1}{\rho^{2}} ds}$$
where $C_{q} = \frac{55}{32\sqrt{3}} \frac{\hbar}{mc} = 3.8 \times 10^{-13} \text{m}$ (for electrons)

where
$$\mathcal{D} = \frac{\oint \frac{1}{\rho^2} \left(2\kappa \rho D + \frac{D}{\rho} \right) ds}{\oint \frac{1}{\rho^2} ds}$$

$$\mathcal{H} = \gamma D^2 + 2\alpha DD' + \beta D'^2$$

For a separated function, isomagnetic machine, this becomes

$$\epsilon_{x}(\infty) = C_{q} \frac{\gamma^{2}}{2\pi\rho_{0}(1-\mathcal{D})} \oint \frac{\mathcal{H}}{\rho} ds$$

With some handwaving, this can be approximated by

$$\epsilon_x(\infty) \approx C_q \gamma^2 \frac{R}{\rho_0} \frac{1}{v_x^3}$$





Robinson's Theorem

Note:

$$\frac{1}{\tau_{\varepsilon}} + \frac{1}{\tau_{x}} + \frac{1}{\tau_{y}} = \frac{U_{s}}{2\tau_{s}E_{s}} (2 + \mathcal{D})$$

$$+ \frac{U_{s}}{2\tau_{s}E_{s}} (1 - \mathcal{D})$$

$$+ \frac{U_{s}}{2\tau_{s}E_{s}}$$

$$= \frac{2U_{s}}{\tau_{s}E_{s}}$$

• This is called Robinson's theorem and it's *always* true. For a separated function, isomagnetic lattice, it simplifies to

$$\frac{1}{\tau_{\varepsilon}} = \frac{U_{s}}{\tau_{s}E_{s}}$$

$$\frac{1}{\tau_{x}} = \frac{1}{\tau_{y}} = \frac{U_{s}}{2\tau_{s}E_{s}}$$





Cheat Sheet Summary

For a separated function, isomagnetic synchrotron

Energy lost per turn
$$\longrightarrow U_s = \frac{e^2 \gamma^4}{3\epsilon_0 \rho_0};$$
 for electrons $U_s [\text{MeV}] = .0885 \frac{E^4 [\text{GeV}]}{\rho_0 [\text{m}]}$

Longitudinal damping time $\longrightarrow \tau_\varepsilon \approx \tau_s \frac{E_s}{U_s}$

$$\tau_x \approx 2\tau_s \frac{E_s}{U_s}$$

Transverse damping times $\tau_x \approx 2\tau_s \frac{E_s}{U_s}$

$$\frac{1}{\tau_\varepsilon} + \frac{1}{\tau_x} + \frac{1}{\tau_y} = \frac{2U_s}{\tau_s E_s} \qquad \text{Robinson's Theorem (always true)}$$

Equilibrium energy spread $\longrightarrow \sigma_\varepsilon^2(\infty) \approx C_q \frac{\gamma^2 E_s^2}{2\rho_0};$ for electrons $C_q = \frac{55}{32\sqrt{3}} \frac{\hbar}{mc} = 3.8 \times 10^{-13} \text{m}$

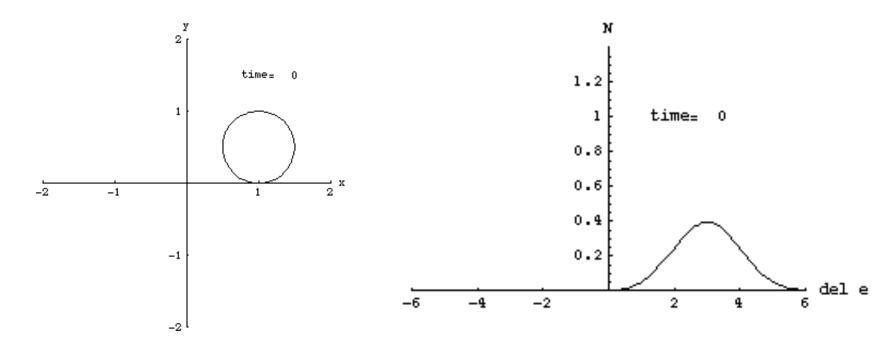
Equilibrium horizontal $\longrightarrow \epsilon_x(\infty) \approx C_q \gamma^2 \frac{R}{\rho_0} \frac{1}{v_x^3}$





Benefits of Damping

- Can inject off orbit and beam will damp down to equilibrium
 - Don't have to worry about painting or charge exchange like protons.
 - Can inject over many turns, or even continuously.
- Beams will naturally "cool" (i.e. reduce their emittance in phase space)
- Example: Beams injected off orbit into CESR







Considerations for e⁺e⁻ Colliders

- In the case of proton-proton and proton-antiproton colliders, we assumed
 - The optics were the same in the two planes
 - The emittances were the same in the two planes
 - The normalized emittance was preserved.
- This allowed us to write

$$L = f \frac{N_b^2}{4\pi\sigma^2} = f_{rev} \frac{1}{4\pi} n_b N_b^2 \frac{\gamma}{\beta^* \epsilon_N}$$

- In general, *none* of this will be true for e⁺e⁻ colliders.
 - The emittance will be much smaller in the y plane
 - Because the emittance is large in the x plane, we will not be able to "squeeze" the optics as far without hitting the aperture in the focusing triplet, so in general, $\beta^*_x > \beta^*_y$.
- We must write

$$L = f \frac{N_1 N_2}{4\pi\sigma_x \sigma_y} = f_{rev} \frac{1}{4\pi} n_b \frac{N_1 N_2}{\sqrt{\beta_x^* \epsilon_x \beta_y^* \epsilon_y}}$$

Unnormalized(!) emittance



Synchrotron Light Sources

- Shortly after the discovery of synchrotron radiation, it was realized that the intense light that was produced could be used for many things
 - Radiography
 - Crystallography
 - Protein dynamics
 - •
- The first "light sources" were parasitic on electron machines that were primarily used for other things.
- As the demand grew, dedicated light sources began to emerge
- The figure or merit is the "brightness"

photons/s/mm² / mrad² / (bandwidth)

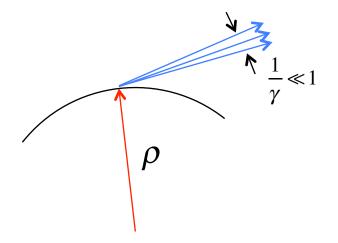




First Generation: Parasitic Operations

These just used the parasitic synchrotron light produced by the

bend dipoles



- Examples
 - SURF (1961): 180 MeV UV synchrotron at NBS
 - CESR (CHESS, 70's): 6 GeV synchrotron at Cornell
 - Numerous others
- Typically large emittances, which limited brightness of the beam





Second Generation: Dedicated

Examples:

1981: 2 GeV SRS at Daresbury (ε=106 nm-rad)

• 1982: 800 MeV BESSY in Berlin (ε=38 nm-rad)

1990: SPEAR II becomes dedicated light source (ε=160 nm-rad)

Often include "wigglers" to enhance SR



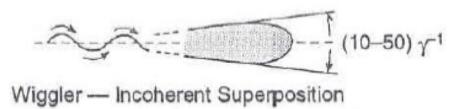


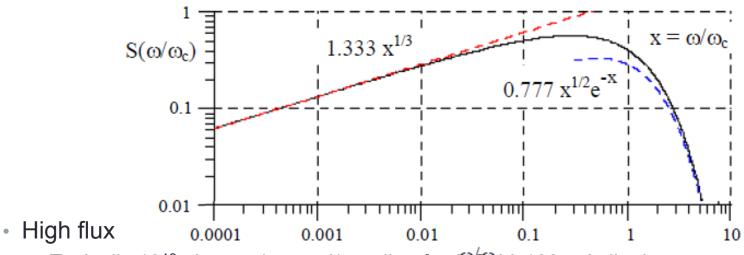




Typical 2nd Generation Parameters

- Beam sizes
 - σ_v~1 mm
 - σ_{v} ~.1 mrad
 - σ_x~.1 mm
 - $\sigma_{x'}$ ~.03 mrad
- Broad spectrum



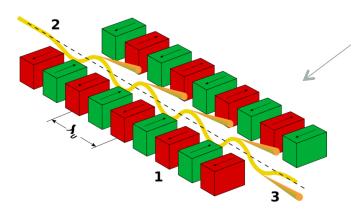


Typically 10¹³ photons/second/mradian for 3°GeV, 100 mA dipole source at E_{crit}





Undulators



Periodic Magnets

In rest frame of electron

$$\lambda^* = \frac{\lambda_U}{\nu}$$

- Electron oscillates coherently with (contracted) structure, and releases photons with the same wavelength.
- In the lab frame, this is Doppler shifted, so

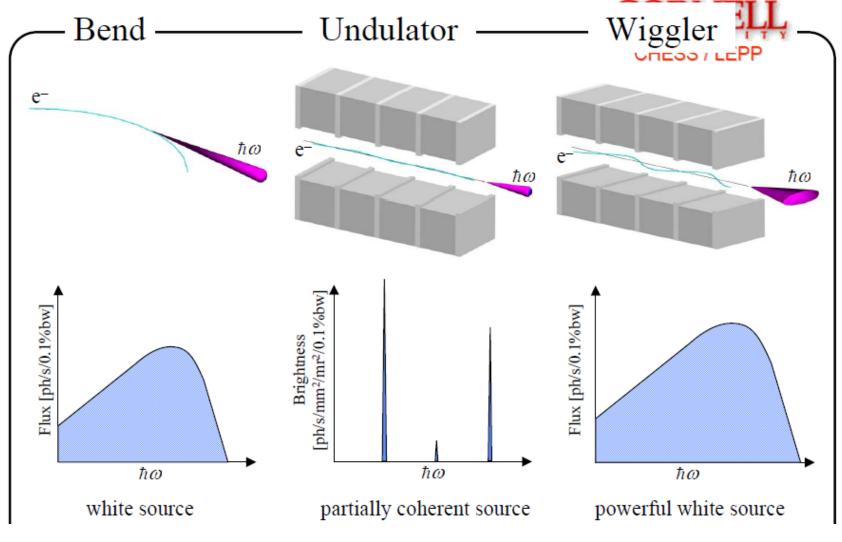
$$\lambda = \frac{\lambda^*}{2\gamma} = \frac{\lambda_U}{2\gamma^2}$$

• So, λ on the order of 1cm \rightarrow X-rays.





Bends, Undulators, and Wigglers*



*G. Krafft





3rd Generation (Undulator) Sources

High Brightness

- 10¹⁹ compared to 10¹⁶ for 2nd generation sources
- Emittance ~1-20 nm-rad

A few Examples:

- CLS
- SPEAR-III
- Soleil
- Diamond
- APS
- PF
- NSLS
- BESSY
- Doris





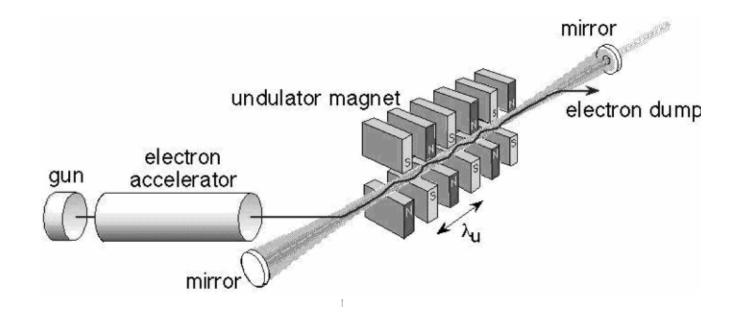
European Synchrotron Radiation Facility (ESRF)





Fourth Generation

 Fourth Generation light sources generally utilize free electron lasers (FELs) to increase brightness by at least an order of magnitude over Third Generation light sources by using coherent production

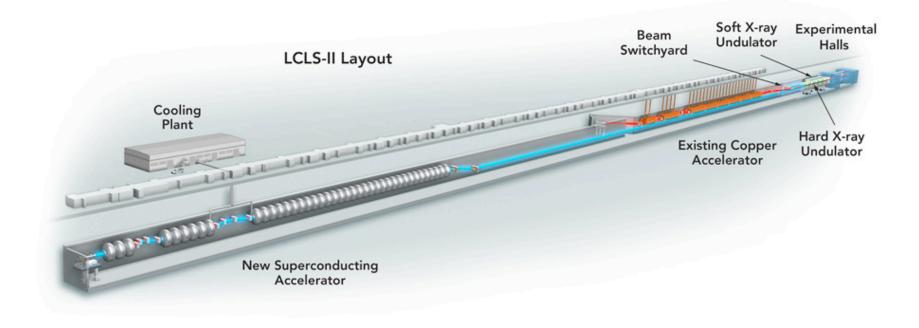






Next Big Thing in the US.

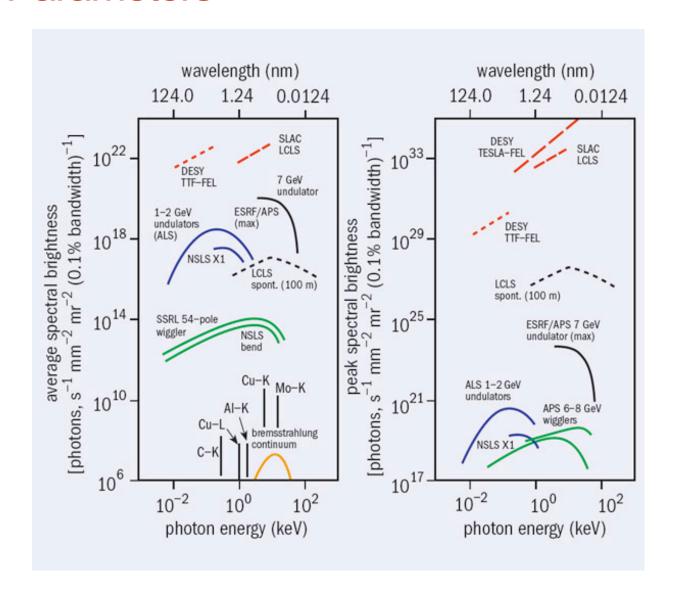
- LCLS-II at SLAC
 - 4 GeV superconducting linac
 - 1 MHz operation
 - X-rays up to 25 keV







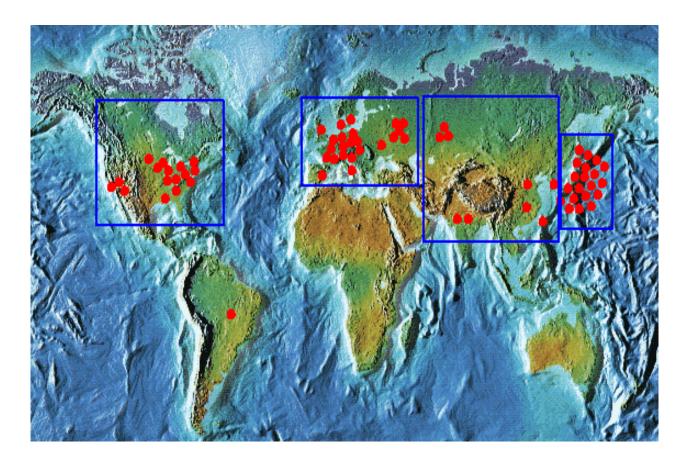
Evolution of Parameters







Light Sources are a Huge (and growing) Industry



Wikipedia lists about 60 light sources worldwide